Abstract—Velocity control of DC motors is an important issue also shorter settling time is desired. In this paper at first a PID compensator which adjusted by genetic algorithm is designed then another compensator will be designed by combining two methods, Integral controller and optimal State Feedback controller (I&S.F.). In the second compensator, design specifications, depend on choosing weighting matrices Q and R, we use the Genetic Algorithm (GA) to find the proper weighting matrices. Of course Kalman filter is used as a system observer in order to increasing the system robustness. Then the performance of the control techniques is compared in terms of rise time, settling time, tracking error, and robustness with respect to modeling errors and disturbances. The controller design process and implementation requirements are also discussed. Then the comparison between the PID control and the optimal controller shows that the optimal controller significantly reduced the overshoot, settling time and has the best performance encountering with system uncertainties. Also we apply noise and 20% parameters variation for DC motor and compare the results. According to the simulation results, the second controller has better performance than the PID controller.

Index Terms—DC Motor, Genetic Algorithm, Kalman Filter, Optimal Control, PID Controller

I. INTRODUCTION

The parameters of an actual DC servomotor used in this paper are listed in Table 1.

<table>
<thead>
<tr>
<th>Table I: MOTOR PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_a$</td>
</tr>
<tr>
<td>$L_a$</td>
</tr>
<tr>
<td>$J$</td>
</tr>
<tr>
<td>$f$</td>
</tr>
<tr>
<td>$K$</td>
</tr>
<tr>
<td>$K_b$</td>
</tr>
</tbody>
</table>

And the transfer function for this DC Motor is:

$$G_p = \frac{0.0147}{7.242e - 006S^2 + 0.000207S + 0.000437}$$

The state space matrices for this system are:

$$A = \begin{bmatrix} -28.58 & -7.542 \\ 8 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 16 \\ 0 \end{bmatrix}$$

$$C = [0 \quad 15.86] \quad D = [0]$$

By this system definition we design the system controller.

II. PID CONTROLLER DESIGN

The conventional PID regulator is the most widely used control strategy in the industry process, because of the remarkable effectiveness, simplicity of implementation and broad applicability. Often in practice, tuning is carried out by an experienced operator using a 'trial and error' procedure and some practical rules, this is often a time consuming and difficult activity.

The objective of a PID controller in a velocity control system is to maintain a velocity set point at a given value and be able to accept new set-point values dynamically. At first a PID controller is designed with genetic algorithm then we show although it has good performance but it is not so robust with system parameters deviation and disturbance and noise in plant [1], [2].

![Fig. 1 A Typical PID Controller System](image)

PID controller Parameters are obtained using a novel genetic algorithm based optimization technique. The conventional integral controller was replaced by a PID controller with the following structure.

$$G_c(s) = \frac{K_p}{s} + \frac{K_i}{s} + K_ds$$

Where $K_p$ is the proportional gain $K_i$ and $K_d$ are integral and derivative time constants respectively. These parameters are selected by genetic algorithm. The fitness function is defined as:
FitnessFunction = \int \left( (e(t))^2 + (u(t))^2 \right) dt

(4)

Where
\( y(t) \): DC Motor velocity (Step response)
\( u(t) \): DC Motor input
\( r(t) \): Reference input (Step function)

\( e(t) \): Error between DC Motor velocity and reference input (it means that smaller \( e(t) \) is desired).

By implying \( u(t) \) in this optimization problem we optimized consumption energy. Step response for this PID has shown in Fig. 2.

Optimal parameters after a complete GA running are shown in Table II [6], [7], [8], and [3].

<table>
<thead>
<tr>
<th>Table II: PID Parameter with GA</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K_p )</td>
</tr>
<tr>
<td>0.496639</td>
</tr>
</tbody>
</table>

III. OPTIMAL INTEGRAL STATE FEEDBACK CONTROLLER DESIGN

At first we design integral controller for the DC motor and then state feedback and Kalman filter are added. We will consider a system defined via minimal state space realization:

\[
\begin{align*}
\dot{x}(t) &= Ax(t) + Bu(t) \\
y(t) &= Cx(t)
\end{align*}
\]

And \( q(t) \) assume by the following definition:

\[
\begin{align*}
\dot{q}(t) &= r - y(t) = r - Cx(t)
\end{align*}
\]

Substituting this equation with equation (7) results in:

\[
\begin{align*}
\dot{q}(t) &= r - Cx(t)
\end{align*}
\]

And the design problem reduces to find the control energy signal \( u(t) \), that given by:

\[
\begin{align*}
u(t) &= - K_1 \dot{x}(t) - K_2 q(t)
\end{align*}
\]

Equations (11), (12) with equation (5) result in:

\[
\begin{align*}
\dot{x}(t) &= A\hat{x}(t) + Bu(t) + L[y(t) - C\hat{x}(t)] \\
y(t) &= [C \ 0] [x(t) \ \hat{x}(t)]
\end{align*}
\]

The block diagram of this controller has shown in Fig. 3.

Least Weighted Vector

We want to design a compensator in order to set-point tracking, and Cost Function will be defined by:

\[
\int ((y(t) - r(t))^T Q (y(t) - r(t)) + u(t)^T R u(t)) dt
\]

(14)

Fig. 3 The Block Diagram of Integral State Feedback Controller with Kalman Filter
energy signal consumption and make tradeoff between energy consumption and system characteristics [4].

IV. GENETIC ALGORITHM APPROACH

The aim of the optimal Linear Quadratic (LQ) tracking is to obtain an optimal control law that minimizes the performance index and forces the plant to track a desired trajectory over a specified time interval. The closed loop performance is related to these weighting matrices. One way to find the proper weighting matrices is a trial- and- error process.

GA as a powerful and broadly applicable stochastic search and optimization techniques is perhaps the most widely known types of evolutionary computation method today [3].

The control law that minimizes Cost Function is given by linear state feedback [5].

\[ k = (R + B^T S B)^{-1} B^T S A \]  
\[ v(k) = (I_{nxn} - A^T + A^T S B (B^T S B + R)^{-1} B^T) C^T Q r(k) \]  
\[ u(k) = (B^T S B + R)^{-1} B^T (-SAx(k) + v(k)) \]  
\[ 0 = A^T S + SA - SBR^{-1}B^T S + C^T QC \]

Weighting matrices \( Q, R \) are found by GA, and then \( u \) can be obtained by solving the Riccati equation (18) and obtaining \( v \) in (16). To apply the GA, we constitute a chromosome with diagonal elements of \( Q, R \) matrices.

The population size was chosen to be 50 and the probability of the crossover and mutation are \( P_c = 0.8, P_m = 0.03 \) respectively.

The best weighting matrices are:

\[ Q = \begin{bmatrix} 8.0135 & 0 \\ 0 & 5.2530 \end{bmatrix}, \quad R = [0.00243] \]

Results show that it has good performance, encountering disturbance, noise and parameters variation in the plant. We combined kalman filter with this controller and results show more robustness performance. System performance for designed controllers has shown in Table III.

Also we apply noise and 20% variation in DC motor parameters and compare the results for two controllers in Fig. 5 and Fig. 6. Error between original plant out-put and plant out-put by applying noise and 20% variation for the PID controller is more than second controller.

V. CONCLUSION

The design and implementation of a PC-based dc motor velocity system using both special optimal control and PID have been presented in this paper, the simulation results reveal that using second controller to the velocity control application, has shorter settling time, and smaller over shoot amplitude. Comparisons of simulation results show that the integral state feedback controller combined by kalman filter due to better robustness performance than the PID controller.

We find the Cost Function optimal weighting matrices \( Q \) and \( R \) by Genetic Algorithm. Simulation results show that by this strategy we have optimal system characteristics (settling time, overshoot amplitude).

According to the simulation results the latest controller has the better performance encountering with noise and disturbance and parameter variation.

![Fig. 4 Step Responses for Second Controller](image1)

![Fig. 5 Errors for PID Controller Applying Noise & 20% Parameter Variation](image2)

![Fig. 6 Errors for Second Controller Applying Noise & 20% Parameter Variation](image3)

| TABLE III: SPEED CONTROLLER PERFORMANCE |
### PID Controller vs. I&S.F. Controller

<table>
<thead>
<tr>
<th>Metric</th>
<th>PID Controller</th>
<th>I&amp;S.F. Controller</th>
</tr>
</thead>
<tbody>
<tr>
<td>Settling Time</td>
<td>0.176 (sec)</td>
<td>0.0748 (sec)</td>
</tr>
<tr>
<td>Overshoot</td>
<td>9.47%</td>
<td>5.16%</td>
</tr>
</tbody>
</table>

### REFERENCES


Mohammad Bagher Banne Sharifian (1965) studied Electrical Power Engineering at the University of Tabriz, Tabriz, Iran. He received the B.Sc. and M.Sc. degrees in 1989 and 1992 respectively from University of Tabriz.

In 1992 he joined the Electrical Engineering Department of the University of Tabriz as a lecturer. He received the Ph.D. degree in Electrical Engineering from the same University in 2000.

In 2000 he rejoined the Electrical Power Department of Faculty of Electrical and Computer of the same university as Assistant Professor. He is currently Associate Professor of the mentioned Department. His research interests are in the areas of design, modeling and analysis of electrical machines, transformers and Electrical Vehicle drives.

Reza Rahnavard received the Msc. degree of Electrical Power Engineering from the University of Tabriz, Tabriz, Iran, in 2007. Currently, he is an Engineer with Azerbaijan Regional Electric Company (A.R.E.C), Tabriz, Iran.

His research interests include power system harmonics, active filtering and application of fuzzy logic theory in power electronic and power systems and MIMO Control applying in power systems.