# Transformerless DC-DC Converters With High Step-Up Voltage Gain 

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#### Abstract

Conventional dc-dc boost converters are unable to provide high step-up voltage gains due to the effect of power switches, rectifier diodes, and the equivalent series resistance of inductors and capacitors. This paper proposes transformerless dc-dc converters to achieve high step-up voltage gain without an extremely high duty ratio. In the proposed converters, two inductors with the same level of inductance are charged in parallel during the switch-on period and are discharged in series during the switch-off period. The structures of the proposed converters are very simple. Only one power stage is used. Moreover, the steady-state analyses of voltage gains and boundary operating conditions are discussed in detail. Finally, a prototype circuit is implemented in the laboratory to verify the performance.


Index Terms-DC-DC boost converter, high step-up voltage gain, power stage.

## I. Introduction

ADC-DC converter with a high step-up voltage gain is used for many applications, such as high-intensitydischarge lamp ballasts for automobile headlamps, fuel-cell energy conversion systems, solar-cell energy conversion systems, and battery backup systems for uninterruptible power supplies. Theoretically, a dc-dc boost converter can achieve a high stepup voltage gain with an extremely high duty ratio [1]-[3]. However, in practice, the step-up voltage gain is limited due to the effect of power switches, rectifier diodes, and the equivalent series resistance (ESR) of inductors and capacitors. Moreover, the extremely high duty-ratio operation will result in a serious reverse-recovery problem. Many topologies have been presented to provide a high step-up voltage gain without an extremely high duty ratio [4]-[24]. A dc-dc flyback converter is a very simple structure with a high step-up voltage gain and an electrical isolation, but the active switch of this converter will suffer a high voltage stress due to the leakage inductance of the transformer. For recycling the energy of the leakage inductance and minimizing the voltage stress on the active switch, some energy-regeneration techniques have been proposed to clamp the voltage stress on the active switch and to recycle the leakage-inductance energy [4]-[6]. The coupled-inductor techniques provide solutions to achieve a high voltage gain, a low voltage stress on the active switch, and a high efficiency without the penalty of high duty ratio [7]-[15]. Literature includes some research of the transformerless dc-dc converters, which include the cascade boost type [16], the quadratic boost

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Fig. 1. Transformerless dc-dc high step-up converter [24].
type [17], the voltage-lift type [18]-[20], the capacitor-diode voltage multiplier type [21], [22], and the boost type integrating with switched-capacitor technique [23]. However, these types are all complex and have a higher cost. The modified boost type with switched-inductor technique is shown in Fig. 1 [24]. The structure of this converter is very simple. Only one power stage is used in this converter. However, this converter has two issues: 1) Three power devices exist in the current-flow path during the switch-on period, and two power devices exist in the currentflow path during the switch-off period, and 2) the voltage stress on the active switch is equal to the output voltage.

A transformerless dc-dc high step-up converter is proposed in this paper, as shown in Fig. 2(a). Compared with the converter in [24], the proposed converter I has the following merits: 1) Two power devices exist in the current-flow path during the switch-on period, and one power device exists in the currentflow path during the switch-off period; 2) the voltage stresses on the active switches are less than the output voltage; and $3)$ under the same operating conditions, including input voltage, output voltage, and output power, the current stress on the active switch during the switch-on period is equal to the half of the current stress on the active switch of the converter in [24]. For getting higher step-up voltage gain, the other dc-dc converters are also presented in this paper, as shown in Fig. 2(b) and (c). These three proposed dc-dc converters utilize the switchedinductor technique, in which two inductors with same level of inductance are charged in parallel during the switch-on period and are discharged in series during the switch-off period, to achieve high step-up voltage gain without the extremely high duty ratio. The operating principles and steady-state analysis are discussed in the following sections. To analyze the steadystate characteristics of the proposed converters, some conditions are assumed as follows: 1) All components are ideal-the ON-state resistance $R_{\mathrm{DS}(\mathrm{ON})}$ of the active switches, the forward voltage drop of the diodes, and the ESRs of the inductors and capacitors are ignored-and 2) all capacitors are sufficiently


Fig. 2. Proposed high step-up dc-dc converters. (a) Converter I. (b) Converter II. (c) Converter III.
large, and the voltages across the capacitors can be treated as constant.

## II. Proposed Converter I

Fig. 2(a) shows the circuit configuration of the proposed converter I, which consists of two active switches ( $S_{1}$ and $S_{2}$ ), two inductors ( $L_{1}$ and $L_{2}$ ) that have the same level of inductance, one output diode $D_{o}$, and one output capacitor $C_{o}$. Switches $S_{1}$ and $S_{2}$ are controlled simultaneously by using one control signal. Fig. 3 shows some typical waveforms obtained during continuous conduction mode (CCM) and discontinuous conduction mode (DCM). The operating principles and steadystate analysis of CCM and DCM are presented in detail as follows.

## A. CCM Operation

The operating modes can be divided into two modes, defined as modes 1 and 2.

(a)

(b)

Fig. 3. Some typical waveforms for the proposed converter I. (a) CCM operation. (b) DCM operation.

1) Mode $1\left[t_{0}, t_{1}\right]$. During this time interval, switches $S_{1}$ and $S_{2}$ are turned on. The equivalent circuit is shown in Fig. 4(a). Inductors $L_{1}$ and $L_{2}$ are charged in parallel from the dc source, and the energy stored in the output capacitor $C_{o}$ is released to the load. Thus, the voltages across $L_{1}$ and $L_{2}$ are given as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=V_{\mathrm{in}} . \tag{1}
\end{equation*}
$$

2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 4(b). The dc source, $L_{1}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. Thus, the voltages across $L_{1}$ and $L_{2}$ are derived as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=\frac{V_{\mathrm{in}}-V_{o}}{2} \tag{2}
\end{equation*}
$$

By using the volt-second balance principle on $L_{1}$ and $L_{2}$, the following equation can be obtained:

$$
\begin{equation*}
\int_{0}^{D T_{s}} V_{\mathrm{in}} d t+\int_{D T_{s}}^{T_{s}} \frac{V_{\mathrm{in}}-V_{o}}{2} d t=0 \tag{3}
\end{equation*}
$$

By simplifying (3), the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{CCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=\frac{1+D}{1-D} \tag{4}
\end{equation*}
$$

From Fig. 3(a), the voltage stresses on $S_{1}, S_{2}$, and $D_{o}$ are derived as

$$
\left\{\begin{array}{l}
V_{S 1}=V_{S 2}=\frac{V_{o}+V_{\mathrm{in}}}{2}  \tag{5}\\
V_{D o}=V_{o}+V_{\mathrm{in}} .
\end{array}\right.
$$

## B. DCM Operation

The operating modes can be divided into three modes, defined as modes 1,2 , and 3 .

1) Mode $1\left[t_{0}, t_{1}\right]$. The operating principle is the same as that for mode 1 of the CCM operation. The two peak currents


Fig. 4. Equivalent circuits of the proposed converter I. (a) Switches ON. (b) Switches OFF. (c) Switches OFF in DCM operation.
of $L_{1}$ and $L_{2}$ can be found as

$$
\begin{equation*}
I_{L 1 p}=I_{L 2 p}=\frac{V_{\mathrm{in}}}{L} D T_{s} \tag{6}
\end{equation*}
$$

where $L$ is the inductance of $L_{1}$ and $L_{2}$.
2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 4(b). The dc source, $L_{1}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. Inductor currents $i_{L 1}$ and $i_{L 2}$ are decreased to zero at $t=t_{2}$. Another expression of $I_{L 1 p}$ and $I_{L 2 p}$ is given as

$$
\begin{equation*}
I_{L 1 p}=I_{L 2 p}=\frac{V_{o}-V_{\mathrm{in}}}{2 L} D_{2} T_{s} \tag{7}
\end{equation*}
$$

3) Mode $3\left[t_{2}, t_{3}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are still turned off. The equivalent circuit is shown in Fig. 4(c). The energies stored in $L_{1}$ and $L_{2}$ are zero. Thus, only the energy stored in $C_{o}$ is discharged to the load.
From (6) and (7), $D_{2}$ is derived as follows:

$$
\begin{equation*}
D_{2}=\frac{2 D V_{\mathrm{in}}}{V_{o}-V_{\mathrm{in}}} \tag{8}
\end{equation*}
$$



Fig. 5. Boundary condition of the proposed converter I.
From Fig. 3(b), the average value of the output-capacitor current during each switching period is given by

$$
\begin{equation*}
I_{c o}=\frac{\frac{1}{2} D_{2} T_{s} I_{L 1 p}-I_{o} T_{s}}{T_{s}}=\frac{1}{2} D_{2} I_{L 1 p}-I_{o} \tag{9}
\end{equation*}
$$

Substituting (6) and (8) into (9), $I_{c o}$ is derived as

$$
\begin{equation*}
I_{c o}=\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-V_{\mathrm{in}}\right)}-\frac{V_{o}}{R} \tag{10}
\end{equation*}
$$

Since $I_{c o}$ is equal to zero under steady state, (10) can be rewritten as follows:

$$
\begin{equation*}
\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-V_{\mathrm{in}}\right)}=\frac{V_{o}}{R} \tag{11}
\end{equation*}
$$

Then, the normalized inductor time constant is defined as

$$
\begin{equation*}
\tau_{L} \equiv \frac{L f_{s}}{R} \tag{12}
\end{equation*}
$$

where $f_{s}$ is the switching frequency $\left(f_{s}=1 / T_{s}\right)$.
Substituting (12) into (11), the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{DCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=\frac{1}{2}+\sqrt{\frac{1}{4}+\frac{D^{2}}{\tau_{L}}} \tag{13}
\end{equation*}
$$

## C. Boundary Operating Condition Between CCM and DCM

If the proposed converter I is operated in boundary conduction mode (BCM), the voltage gain of the CCM operation is equal to the voltage gain of the DCM operation. From (4) and (13), the boundary normalized inductor time constant $\tau_{L B}$ can be derived as follows:

$$
\begin{equation*}
\tau_{L B}=\frac{D(1-D)^{2}}{2(1+D)} \tag{14}
\end{equation*}
$$

The curve of $\tau_{L B}$ is shown in Fig. 5. If $\tau_{L}$ is larger than $\tau_{L B}$, the proposed converter I is operated in CCM.

## III. Proposed Converter II

Fig. 2(b) shows the circuit configuration of the proposed converter II, which is the proposed converter I with one voltage-lift


Fig. 6. Some typical waveforms for the proposed converter II. (a) CCM operation. (b) DCM operation.
circuit [18]-[20]. Thus, two inductors ( $L_{1}$ and $L_{2}$ ) with the same level of inductance are also adopted in this converter. Switches $S_{1}$ and $S_{2}$ are controlled simultaneously by one control signal. Fig. 6 shows some typical waveforms of CCM and DCM. Moreover, the operating principles and steady-state analysis of CCM and DCM are presented as follows.

## A. CCM Operation

The operating modes can be divided into two modes, defined as modes 1 and 2.

1) Mode $1\left[t_{0}, t_{1}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned on. The equivalent circuit is shown in Fig. 7(a). $L_{1}$ and $L_{2}$ are charged in parallel from the dc source, and the energy stored in $C_{o}$ is released to the load. Moreover, capacitor $C_{1}$ is charged from the dc source. Thus, the voltages across $L_{1}, L_{2}$, and $C_{1}$ are given as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=V_{C 1}=V_{\mathrm{in}} \tag{15}
\end{equation*}
$$

2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 7(b). The dc source, $L_{1}, C_{1}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. Thus, the voltages across $L_{1}$ and $L_{2}$ are derived as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=\frac{V_{\mathrm{in}}+V_{c 1}-V_{o}}{2}=\frac{2 V_{\mathrm{in}}-V_{o}}{2} \tag{16}
\end{equation*}
$$

By using the volt-second balance principle on $L_{1}$ and $L_{2}$, the following can be obtained:

$$
\begin{equation*}
\int_{0}^{D T_{s}} V_{\mathrm{in}} d t+\int_{D T_{s}}^{T_{s}} \frac{2 V_{\mathrm{in}}-V_{o}}{2} d t=0 \tag{17}
\end{equation*}
$$

By simplifying (17), the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{CCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=\frac{2}{1-D} \tag{18}
\end{equation*}
$$



Fig. 7. Equivalent circuits of the proposed converter II. (a) Switches ON. (b) Switches OFF. (c) Switches OFF in DCM operation.

From Fig. 6(a), the voltage stresses on $S_{1}, S_{2}, D_{1}$, and $D_{o}$ are derived as

$$
\left\{\begin{array}{l}
V_{S 1}=V_{S 2}=V_{D 1}=\frac{V_{o}}{2}  \tag{19}\\
V_{D o}=V_{o}
\end{array}\right.
$$

## B. DCM Operation

The operating modes can be divided into three modes, defined as modes 1,2 , and 3 .

1) Mode $1\left[t_{0}, t_{1}\right]$. The operating principle is the same as that for mode 1 of the CCM operation. The two peak currents of $L_{1}$ and $L_{2}$ can be found as

$$
\begin{equation*}
I_{L 1 p}=I_{L 2 p}=\frac{V_{\mathrm{in}}}{L} D T_{s} \tag{20}
\end{equation*}
$$

2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 7(b).

The dc source, $L_{1}, C_{1}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. The values for $i_{L 1}$ and $i_{L 2}$ are decreased to zero at $t=t_{2}$. Another expression for $I_{L 1 p}$ and $I_{L 2 p}$ is given as

$$
\begin{equation*}
I_{L 1 p}=I_{L 2 p}=\frac{V_{o}-V_{\mathrm{in}}-V_{c 1}}{2 L} D_{2} T_{s}=\frac{V_{o}-2 V_{\mathrm{in}}}{2 L} D_{2} T_{s} \tag{21}
\end{equation*}
$$

3) Mode $3\left[t_{2}, t_{3}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are still turned off. The equivalent circuit is shown in Fig. 7(c). The energies stored in $L_{1}$ and $L_{2}$ are zero. Thus, only the energy stored in $C_{o}$ is discharged to the load.
From (20) and (21), $D_{2}$ is derived as follows:

$$
\begin{equation*}
D_{2}=\frac{2 D V_{\mathrm{in}}}{V_{o}-2 V_{\mathrm{in}}} \tag{22}
\end{equation*}
$$

From Fig. 6(b), the average output-capacitor current during each switching period is given by

$$
\begin{equation*}
I_{c o}=\frac{\frac{1}{2} D_{2} T_{s} I_{L 1 p}-I_{o} T_{s}}{T_{s}}=\frac{1}{2} D_{2} I_{L 1 p}-I_{o} \tag{23}
\end{equation*}
$$

By substituting (20) and (22) into (23), $I_{c o}$ is derived as

$$
\begin{equation*}
I_{c o}=\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-2 V_{\mathrm{in}}\right)}-\frac{V_{o}}{R} . \tag{24}
\end{equation*}
$$

Since $I_{c o}$ is equal to zero under steady state, (24) can be rewritten as follows:

$$
\begin{equation*}
\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-2 V_{\mathrm{in}}\right)}=\frac{V_{o}}{R} \tag{25}
\end{equation*}
$$

Thus, the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{DCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=1+\sqrt{1+\frac{D^{2}}{\tau_{L}}} \tag{26}
\end{equation*}
$$

## C. Boundary Operating Condition Between CCM and DCM

If the proposed converter II is operated in BCM, the voltage gain of the CCM operation is equal to the voltage gain of the DCM operation. From (18) and (26), the boundary normalized inductor time constant $\tau_{L B}$ can be derived as

$$
\begin{equation*}
\tau_{L B}=\frac{D(1-D)^{2}}{4} \tag{27}
\end{equation*}
$$

The curve of $\tau_{L B}$ is shown in Fig. 8. If $\tau_{L}$ is larger than $\tau_{L B}$, the proposed converter II is operated in CCM.

## IV. Proposed Converter III

Fig. 2(c) shows the circuit configuration of the proposed converter III, which is the proposed converter I with two voltagelift circuits. Thus, two inductors ( $L_{1}$ and $L_{2}$ ) with the same level of inductance are also adopted in this converter. Switches $S_{1}$ and $S_{2}$ are controlled simultaneously by one control signal. Fig. 9 shows some typical waveforms of CCM and DCM.


Fig. 8. Boundary condition of the proposed converter II.


Fig. 9. Some typical waveforms for the proposed converter III. (a) CCM operation. (b) DCM operation.

Moreover, the operating principles and steady-state analysis of CCM and DCM are presented as follows.

## A. CCM Operation

The operating modes can be divided into two modes, defined as modes 1 and 2.

1) Mode $1\left[t_{0}, t_{1}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned on. The equivalent circuit is shown in Fig. 10(a). $L_{1}$ and $L_{2}$ are charged in parallel from the dc source, and the energy stored in $C_{o}$ is released to the load. Moreover, capacitors $C_{1}$ and $C_{2}$ are charged from the dc source. Thus, the voltages across $L_{1}, L_{2}, C_{1}$, and $C_{2}$ are given as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=V_{C 1}=V_{C 2}=V_{\mathrm{in}} \tag{28}
\end{equation*}
$$

2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 10(b). The dc source, $L_{1}, C_{1}, C_{2}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. Thus, the voltages across $L_{1}$ and $L_{2}$ are derived as

$$
\begin{equation*}
\nu_{L 1}=\nu_{L 2}=\frac{V_{\mathrm{in}}+V_{c 1}+V_{c 2}-V_{o}}{2}=\frac{3 V_{\mathrm{in}}-V_{o}}{2} \tag{29}
\end{equation*}
$$



Fig. 10. Equivalent circuits of the proposed converter III. (a) Switches ON. (b) Switches OFF. (c) Switches OFF in DCM operation.

By using the volt-second balance principle on $L_{1}$ and $L_{2}$, the following can be obtained:

$$
\begin{equation*}
\int_{0}^{D T_{s}} V_{\mathrm{in}} d t+\int_{D T_{s}}^{T_{s}} \frac{3 V_{\mathrm{in}}-V_{o}}{2} d t=0 \tag{30}
\end{equation*}
$$

By simplifying (30), the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{CCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=\frac{3-D}{1-D} \tag{31}
\end{equation*}
$$

From Fig. 9(a), the voltage stresses on $S_{1}, S_{2}, D_{1}, D_{2}$, and $D_{o}$ are derived as

$$
\left\{\begin{array}{l}
V_{S 1}=V_{S 2}=V_{D 1}=V_{D 2}=\frac{V_{o}-V_{\mathrm{in}}}{2}  \tag{32}\\
V_{D o}=V_{o}-V_{\mathrm{in}} .
\end{array}\right.
$$

## B. DCM Operation

The operating modes can be divided into three modes, defined as modes 1,2 , and 3 .

1) Mode $1\left[t_{0}, t_{1}\right]$. The operating principle is the same as that for mode 1 of CCM operation. The two peak currents of
$L_{1}$ and $L_{2}$ can be found as

$$
\begin{equation*}
I_{L 1 p}=I_{L 2 p}=\frac{V_{\mathrm{in}}}{L} D T_{s} \tag{33}
\end{equation*}
$$

2) Mode $2\left[t_{1}, t_{2}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are turned off. The equivalent circuit is shown in Fig. 10(b). The dc source, $L_{1}, C_{1}, C_{2}$, and $L_{2}$ are series connected to transfer the energies to $C_{o}$ and the load. The values for $i_{L 1}$ and $i_{L 2}$ are decreased to zero at $t=t_{2}$. Another expression for $I_{L 1 p}$ and $I_{L 2 p}$ is given as

$$
\begin{align*}
I_{L 1 p} & =I_{L 2 p}=\frac{V_{o}-V_{\mathrm{in}}-V_{c 1}-V_{c 2}}{2 L} D_{2} T_{s} \\
& =\frac{V_{o}-3 V_{\mathrm{in}}}{2 L} D_{2} T_{s} . \tag{34}
\end{align*}
$$

3) Mode $3\left[t_{2}, t_{3}\right]$. During this time interval, $S_{1}$ and $S_{2}$ are still turned off. The equivalent circuit is shown in Fig. 10(c). The energies stored in $L_{1}$ and $L_{2}$ are zero. Thus, only the energy stored in $C_{o}$ is discharged to the load.
From (33) and (34), $D_{2}$ is derived as follows:

$$
\begin{equation*}
D_{2}=\frac{2 D V_{\mathrm{in}}}{V_{o}-3 V_{\mathrm{in}}} \tag{35}
\end{equation*}
$$

From Fig. 9(b), the average output-capacitor current during each switching period is given by

$$
\begin{equation*}
I_{c o}=\frac{\frac{1}{2} D_{2} T_{s} I_{L 1 p}-I_{o} T_{s}}{T_{s}}=\frac{1}{2} D_{2} I_{L 1 p}-I_{o} \tag{36}
\end{equation*}
$$

By substituting (33) and (35) into (36), $I_{c o}$ is derived as

$$
\begin{equation*}
I_{c o}=\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-3 V_{\mathrm{in}}\right)}-\frac{V_{o}}{R} \tag{37}
\end{equation*}
$$

Since $I_{c o}$ is equal to zero under steady state, (37) can be rewritten as follows:

$$
\begin{equation*}
\frac{D^{2} V_{\mathrm{in}}^{2} T_{s}}{L\left(V_{o}-3 V_{\mathrm{in}}\right)}=\frac{V_{o}}{R} \tag{38}
\end{equation*}
$$

Thus, the voltage gain is given by

$$
\begin{equation*}
M_{\mathrm{DCM}}=\frac{V_{o}}{V_{\mathrm{in}}}=\frac{3}{2}+\sqrt{\frac{9}{4}+\frac{D^{2}}{\tau_{L}}} \tag{39}
\end{equation*}
$$

## C. Boundary Operating Condition Between CCM and DCM

If the proposed converter III is operated in BCM, the voltage gain of CCM operation is equal to the voltage gain of DCM operation. From (31) and (39), the boundary normalized inductor time constant $\tau_{L B}$ can be derived as follows:

$$
\begin{equation*}
\tau_{L B}=\frac{D(1-D)^{2}}{2(3-D)} \tag{40}
\end{equation*}
$$

The drawing of $\tau_{L B}$ is shown in Fig. 11. If $\tau_{L}$ is larger than $\tau_{L B}$, the proposed converter III is operated in CCM.


Fig. 11. Boundary condition of the proposed converter III.
TABLE I
Comparison of Voltage Gain and Voltage Stress on Active Switch for Boost Converter and Three Proposed Converters

|  | $M_{C C M}$ | Voltage stress |
| :---: | :---: | :---: |
| Boost converter | $\frac{1}{1-D}$ | $V_{o}$ |
| Proposed converter I | $\frac{1+D}{1-D}$ | $\frac{V_{o}+V_{i n}}{2}$ |
| Proposed converter II | $\frac{2}{1-D}$ | $\frac{V_{o}}{2}$ |
| Proposed converter III | $\frac{3-D}{1-D}$ | $\frac{V_{o}-V_{i n}}{2}$ |



Fig. 12. Voltage gain versus duty ratio for the boost converter and the three proposed converters.

## V. Comparison of Proposed Converters and Boost Converter

The voltage stresses on the active switch and the voltage gains of the boost converter and the proposed converters are summarized in Table I. The voltage stresses on the active switch of the three proposed converters are less than the voltage stress on the active switch of the boost converter, and thus, the active switches with low voltage ratings and low ON-state resistance levels $R_{D S(O N)}$ can be selected. Moreover, the curves of the voltage gain of the boost converter and the proposed converters


Fig. 13. Some experimental waveforms of the proposed converter I. (a) $i_{\text {in }}$, $i_{L 1}$, and $i_{L 2}$. (b) $i_{S 1}$ and $i_{S 2}$. (c) $\nu_{S 1}$ and $\nu_{S 2}$. (d) $\nu_{D o}$ and $i_{D o}$.
are shown in Fig. 12. As illustrated, the proposed converters can achieve high step-up voltage gain.

## VI. Experimental Results

To verify the theoretical analyses of the proposed converter I, a $40-\mathrm{W}$ prototype circuit is built in the laboratory for use in an automobile headlamp application. The circuit specifications

(a)

(b)

Fig. 14. Dynamic response of the proposed converter I. (a) $P_{o}$ is charged from 5 to 40 W . (b) $P_{o}$ is charged from 40 to 5 W .


Fig. 15. Ideal and experimental voltage gains of the proposed converter I under $V_{\text {in }}=12 \mathrm{~V}, V_{o}=60-100 \mathrm{~V}$, and $P_{o}=40 \mathrm{~W}$.


Fig. 16. Experimental efficiency of the proposed converter I and the converter in [24] under $V_{\mathrm{in}}=12 \mathrm{~V}, V_{o}=60-100 \mathrm{~V}$, and $P_{o}=40 \mathrm{~W}$.
and components are selected as $V_{\mathrm{in}}=12 \mathrm{~V}, V_{o}=60-100 \mathrm{~V}$, $f_{s}=100 \mathrm{kHz}, P_{o}=40 \mathrm{~W}, L_{1}=L_{2}=100 \mu \mathrm{H}$, and $C_{o}=$ $68 \mu \mathrm{~F}$. Moreover, MOSFET NTY100N10 is selected for switches $S_{1}$ and $S_{2}$, and the Schottky diode MBR20200CT is selected for diode $D_{o}$.

Under the conditions $V_{\mathrm{in}}=12 \mathrm{~V}, V_{o}=100 \mathrm{~V}$, and $P_{o}=$ 40 W , some experimental results are shown in Fig. 13. Fig. 13(a) shows that $i_{L 1}$ is equal to $i_{L 2}$. Moreover, the input current is equal to twice the level of the inductor current during the switch-on period and is equal to the inductor current during the switch-off period. Fig. 13(b) shows the current waveforms $i_{S 1}$ and $i_{S 2}$. As can be seen in Fig. 13(c), the voltage stresses on $S_{1}$ and $S_{2}$ are equal to $\left(V_{o}+V_{\text {in }}\right) / 2$. Fig. 13(d) shows the voltage and current of the output diode. Fig. 14 shows the dynamic response under the output power variation between $5-\mathrm{W}$ light load and $40-\mathrm{W}$ full load. One can see that the output voltage is well regulated. Fig. 15 shows the ideal and experimental voltage gains under $V_{\text {in }}=12 \mathrm{~V}, V_{o}=60-100 \mathrm{~V}$, and $P_{o}=40 \mathrm{~W}$. Fig. 16 shows the experimental efficiency of the proposed converter I and the converter in [24] under $V_{\text {in }}=12 \mathrm{~V}, V_{o}=60-100 \mathrm{~V}$, and $P_{o}=40 \mathrm{~W}$. It is seen that the proposed converter I has higher efficiency than the converter in [24].

## VII. Conclusion

This paper has studied three novel transformerless dc-dc converters with high step-up voltage gain. The structures of the proposed converters are very simple. Since the voltage stresses on the active switches are low, active switches with low voltage ratings and low ON-state resistance levels $R_{\mathrm{DS}(\mathrm{ON})}$ can be selected. The steady-state analyses of the voltage gain and the boundary operating condition are discussed in detail. Finally, to illustrate the theoretical analysis, a 40-W prototype circuit of the proposed converter I is built in the laboratory. The experimental results confirm that high step-up voltage gain can be achieved.

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